School of Science, Assignment Session 2022-23

Course Code: UGMM -101 Course Title: Differential Calculus Maximum Marks : 30

(Section 'A')

(Long Answer Questions)

NOTE: Answer each question in 500 to 800 words. All carry equal marks.

Maximum Marks: 18

- 1. Let f be defined on R such that f(x) = 0 and $f(x) = \frac{e^{1/x}}{1 + e^{1/x}}$ when $x \neq 0$ Does limt exit when $x \to 0$
- 2. Let f be defined on R such that f(x) = 5x 4 when $0 \le x \le 1$ $f(x) = 4x^2 - 3$ when $1 \le x \le 2$ f(x) = 5x + 4 when x > 2

is f continuous at x = 1 and x = 2?

3. Show that if faction is differentiable at given point then it is continuous at that point. is the converse true ? Support your answer.

(Section – B)

(Short Answer Questions)

Maximum Marks: 12

- 4. Let R be a relation defined in the set of natural numbers N such that $R = \{(x, y): 3x + y = 15\}$ find the domain and range of R.
- 5. Let $f: \mathbb{R} \to \mathbb{R}$ be a map defined by $f(x) = x^2$ and

let
$$A = \{x \in \mathbb{R} : 1 \le x \le 2\}$$
 find $f(A)$

- 6. If fx = 2x 1 and g(x) = x + 4 then find (f.g)(x).
- 7. Consider a map $f: \mathbb{R} \to \mathbb{R}$ such that $f(x) = 4x^2 3$ is f injective.

School of Science, Assignment Session 2022-23

Course Code: UGMM-102 Course Title: Analytical Geometry Maximum Marks : 30

(Section 'A')

(Long Answer Questions)

NOTE: Answer each question in 500 to 800 words. All carry equal marks.

Maximum Marks: 18

- 1. Find the point of intersection of the line $\frac{x+1}{1} = \frac{y+3}{3} = \frac{z-2}{2}$ with the plain 3x + 4y + z = 10
- 2. Find the equation of the sphere for which the circle $x^2 + y^2 + z^2 + 7y - 2z + 2 = 0$, 2x + 3y + 4z = 8 is a great circle.
- 3. Find the equation of the tenant plains of the sphere $x^2 + y^2 + z^2 2x + 4y 6z + 30 = 0$ which are parallel 2x y + z = 0

(Section – B)

(Short Answer Questions)

Maximum Marks: 12

Note: Answer each question in 200 to 300 Words. All carry equal marks.

4. If the equation $x^2 - y^2 - 2x + 2y + \lambda = 0$

represent a degenerate conic then find the value of λ

- 5. Find the angle between the pair of straight lines $x^2 + 4y^2 7xy = 0$
- 6. Find the perpendicular distance from the origin to the plain x + 2y + z = 3 also find the direction cosines of the normal to the plain.
- 7. Find the angle between the planes 2x y + z = 5 and x + 3y + 2z = 7

School of Science, Assignment Session 2022-23

Course Code: UGMM-103 Course Title: Integral Calculus Maximum Marks : 30

(Section 'A')

(Long Answer Questions)

NOTE: Answer each question in 500 to 800 words. All carry equal marks.

Maximum Marks: 18

- 1. Show that xy = 1 and $x^2 + y^2 = 2$ tuch each other at two points.
- 2. Under what condition the curves $a_1x^2 + b_1y^2 = 1$ and $a_2x^2 + b_2y^2 = 1$ cut orthogonally
- 3. Find the angle of the intersection of the curves $y^2 = x$ and $x^2 + y^2 = 4$

(Section – B)

(Short Answer Questions)

Maximum Marks: 12

- 4. Show that $\int_0^{\pi/2} (\sin^2 x) \cos x \, dx = \frac{1}{3}$
- 5. Integrate $e^{ten x} \cdot sec^2 x \quad w.r.t. \quad x$
- 6. Evaluate $\int_0^{\pi/4} (ten^5 x) dx$
- 7. Integrate $\frac{\sqrt{x}}{1+x^{1/4}}$ w.r.t. x

School of Science, Assignment Session 2022-23

Course Code: UGMM-104 Course Title: Differential Equation Maximum Marks : 30

(Section 'A')

(Long Answer Questions)

NOTE: Answer each question in 500 to 800 words. All carry equal marks.

Maximum Marks: 18

1. Solve that differential equation

 $(1 + 4xy + 2y^2)dx + (1 + 4xy + 2x^2) dy = 0$

- 2. Solve $x^2 + p^2 x = yp$
- 3. Find the orthogonal trajectories of the cardiod $r = a(1 \cos \theta)$, a being the parameter.

(Section – B)

(Short Answer Questions)

Maximum Marks: 12

- 4. Solve $\frac{dy}{dx} = e^{x-y} + x^2 e^{-y}$
- 5. Solve $x \cdot Dy + y = xy^3$
- 6. Solve y = cx + a/c
- 7. Is the following equation excel $(1 + e^{x/y})dx + e^{x/y}(1 x/y)dy = 0$

School of Science, Assignment Session 2022-23

Course Code: UGMM-105	Course Title: Mechanics-I (Statics and	Maximum Marks : 30
	Dynamics)	

(Section 'A')

(Long Answer Questions)

NOTE: Answer each question in 500 to 800 words. All carry equal marks.

Maximum Marks: 18

- 1. If *T* be the tension at any point P of a common catenary and *To* be the tension at the lowest point *A* then prove that $T^2 To^2 = W^2$ when *W* in the weight of the are AP of the cetenery.
- 2. Five weight less rods of equal length are joined together so as to from a rhombus ABCD with one diagonal *BD*. at a weight *W* be attached to *C* and the system be suspended from *A* then show that there is a thrust in *BD* equal $w/\sqrt{3}$.
- 3. The velocities of a pastiche along and perpendicular to the radius vector from a fixed point are $\times r \& \mu \theta$. Find the path of the particle.

(Section – B)

(Short Answer Questions)

Maximum Marks: 12

- 4. A particle is allowed to move from the top of a cycloid whose vertex is upward and plane vertical with negligible velocity. Find the point where the particle leaves the cycloid.
- 5. A body consisting at a core and a hemisphere on the same base rests on a rough horizontal table the hemisphere being in contact with the table of the height of the cone is $\sqrt{3}$ times the radius of the hemisphere . Find whether the equilibrium will be stable or unstable.
- 6. A particle moves with a central acceleration which varies inversely as the cube of the distance if it is projected from an apse at a distance a from the origin with velocity which is $\sqrt{2}$ time of the velocity for a circle of radius a then show that its path is $r \cos \frac{\theta}{\sqrt{2}} = a$.
- 7. A particle whose mass is m is acted upon by a force $m\mu\left(x + \frac{a^4}{x^3}\right)$ towards the origin if it stats from rest a distance a then show that it will arrive at the origin is time $\frac{\pi}{4\sqrt{\mu}}$

School of Science, Assignment Session 2022-23

Course Code: UGMM-106	Course Title: Mechanics-II (Dynamics and	Maximum Marks : 30
	Hydrodynamics)	

(Section 'A')

(Long Answer Questions)

NOTE: Answer each question in 500 to 800 words. All carry equal marks.

Maximum Marks: 18

- 1. Find the moment of inertia of a rod of length 2a & mass M about a line through its centre perpendicular to *its* length.
- 2. Find the moment of inertia of a circular disc of radian 'a' about *its* diametre.
- 3. At the vertex c of a tangle ABC which is a right angle at c show that the principle axis in the plane are inclined to the sides at an angle $\frac{1}{2} \tan^{-1} \frac{ab}{a^2 b^2}$.

(Section – B)

(Short Answer Questions)

Maximum Marks: 12

- 4. One end of a light string is fixed to a point of the rim of a uniform circular disc of radian 'a' & mass 'm' and the string is wound several times round the rim. the free end is attached to a fixed point and the disc is held so that the part of the string not in contact with the vertical of the disc be let go find the acceleration & tension of the string.
- 5. Find the moment of inertia of a right circular cylinder about a straight line through its centre of gravity perpendicular to its axis.
- 6. A straight uniform rod can turn freely about one end O, hangs from O vertically. Find the least angular velocity with which it must begin to moves so that it may perform complete revolution in a vertical plane.
- 7. Show that the moment of inertia of the area bounded by $r^2 = a^2 cos \ 2\theta$ about its axis is

$$\frac{Ma^2}{16}(\pi - 8/3)$$

School of Science, Assignment Session 2022-23

Course Code: UGMM-107 Course Title: Linear Algebra Maximum Marks : 30

(Section 'A')

(Long Answer Questions)

NOTE: Answer each question in 500 to 800 words. All carry equal marks.

Maximum Marks: 18

- 1. Find all eign values and eign vectors of a linear transformation $T : IR^3 IR^3$, defined as T(x, y, z) = (2x + y, y - z, 2y + 4z). Is T diagonolizatble
- 2. If w_1 and w_2 are any two finite subspaces of a vector space V then show that

$$dim (w_1 + w_2) = dim w_1 + dim w_2 - dim (w_1 \cap w_2)$$
3. Find the eigen Values and eigen vectors of the matrix
$$A = \begin{pmatrix} 1 & 1 & 3 \\ 3 & 2 & 4 \\ 3 & 4 & 5 \end{pmatrix}$$

(Section – B)

(Short Answer Questions)

Maximum Marks: 12

Note: Answer each question in 200 to 300 Words. All carry equal marks.

4. Let V be a vector space over a field F such that it has no proper subspace. Then show that either

 $V = \{ o \} or dim V = 1.$

- 5. Which of the following is a linear transformation where T : IR² → IR²

 (a) T (x1, x2) = (1 + x1, x2)
 (b) T (x1, x2) = (x2, x1)

 6. A function f is defined on IR² as follows:
 - $f(x,y) = (x_1 y_1)^2 + x_1 y_2, where x = (x_1 x_2) and y = (y_1, y_2)$ Is f a bilinear forms? Verify.

School of Science, Assignment Session 2022-23

Course Code: UGMM-108	Course Title: Calculus of function of	Maximum Marks : 30
	several variable and Vector Calculus	

(Section 'A')

(Long Answer Questions)

NOTE: Answer each question in 500 to 800 words. All carry equal marks.

Maximum Marks: 18

- 1. at $u = e^{xyz}$ then show that $\frac{\partial^3 u}{\partial x \partial y \partial z} = (1 + 3xyz + x^2y^2z^2)$ is it also equal to $\frac{\partial^3 u}{\partial y \partial z \partial x}$?
- 2. Show that $\frac{\partial(u,v)}{\partial(x,y)} \times \frac{\partial(x,y)}{\partial(u,v)} = 1$
- 3. A particle moves so that its position vector in given by $\bar{r} = \hat{\iota} \cos wt + \hat{j} \sin wt$ Show that the velocity \bar{v} is perpendicular \bar{r} and $\bar{r} \times \bar{v}$ is constant vector.

(Section – B)

(Short Answer Questions)

Maximum Marks: 12

Note: Answer each question in 200 to 300 Words. All carry equal marks.

4. Find the deviational derivative of $f(x) = xy^2 + yz^3$ at the point (1, -1, 1) along the vector $\hat{i} + 2\hat{j} + 2\hat{k}$

5. at $u = \tan^{-1}\left(\frac{x^3 + y^3}{x - y}\right)$ then show that $x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y} = \sin 2u$

- 6. Determine the point where the function $x^4 + y^4 2x^2 + 4xy 2y^2$ has a maximum are minimum.
- 7. Find curl (curl \overline{F}) at the point (0,1,2) where $\overline{F} = (x^2y)\hat{\iota} + (xyz)\hat{J} + (z^2y)\hat{k}$

Evaluate $\int \overline{F} d\overline{r}$ whre $\overline{F} = (3x^2)\hat{i} + (2xz - y)\hat{j} + z\hat{k}$ along the straight line joinery (0,0,0) & (2,1,3)

School of Science, Assignment Session 2021-22

Course Code: DCEMM-109 Course Title: Abstract Algebra Maximum Marks : 30

(Section 'A')

(Long Answer Questions)

NOTE: Answer each question in 500 to 800 words. All carry equal marks.

Maximum Marks: 18

- 1. State and Prove fundamental theorem of group homomorphism.
- Let N be a normal subgroups of a group G and H be a subgroup of G then show that:
 (i) H ∩ N is normal subgroup of H (ii) HN is a subgroup of G (iii) N is normal subgroup of HN.
- 3. Prove that if G is abelian then $G|_{Z(G)}$ is cyclic where Z(G) is centre of G.

(Section – B)

(Short Answer Questions)

Maximum Marks: 12

- 4. Give all sub groups of $(Z_{12}, +)$
- 5. Let $f: G_{11} \to G_2$ be a group homomorphism then show that kernel f is a normal subgroup of G_1 .
- 6. Give an example non-cycle group whose all subgroups are cyclic.
- 7. Find all zero divisor elements of Z/20.

School of Science, Assignment Session 2021-22

Course Code: DCEMM-110 Course Title: Number Theory Maximum Marks : 30

(Section 'A')

(Long Answer Questions)

NOTE: Answer each question in 500 to 800 words. All carry equal marks.

Maximum Marks: 18

1. Find the remainders obtained on division of the following:

(a) 3⁵⁰ by 101 (b) 159⁷⁶⁵⁴ by 23

2. Find the g.c.d. of 163 and 34 and express it in the form 163m +

34*n* in two ways.

3. Prove that (a) $18! + 1 \equiv 0 \pmod{437}$ (b) $28! + 233 \equiv 0 \pmod{899}$.

(Section – B)

(Short Answer Questions)

Maximum Marks: 12

- **4.** Show that every square is congruent to 0 or 1 (mod 8).
- 5. Find the value of $\phi(m)$ if m = 500.
- 6. Find the following Legendre symbols: (a) $\begin{pmatrix} 19\\ 41 \end{pmatrix}$ (b) $\begin{pmatrix} 3\\ 7 \end{pmatrix}$ (c) $\begin{pmatrix} 5\\ 11 \end{pmatrix}$ (d) $\begin{pmatrix} 6\\ 11 \end{pmatrix}$
- 7. Find the value of Mobius function $\mu(n)$ for n
 - (a) 15 (b) 30 (c) 47 (d) 100

School of Science, Assignment Session 2021-22

Course Code: DCEMM-112 Course Title: Advance Analysis Maximum Marks : 30

(Section 'A')

(Long Answer Questions)

NOTE: Answer each question in 500 to 800 words. All carry equal marks.

Maximum Marks: 18

- **1.** Every Cauchy sequence (S_n) of real Numbers converges.
- 2. Let (X_1, d_1) and (X_2, d_2) be two discrete metric spaces. Then verify that the product metric on $X_1 \ge X_2$ is discrete.
- 3. Show that a Cauchy sequence is convergent⇔ it has a convergent subsequence.
- 4. Let (X, d) be a metric space and $A \subseteq X$. Show that $\overline{A} = \{x \in X : d(x, A) = 0\}$.

(Section – B)

(Short Answer Questions)

Maximum Marks: 12

Note : Answer each question in 200 to 300 Words. All carry equal marks.

5. Define Complete Metric Space. Given an example of a metric space which is not Complete.

6. Any compact metric space is totally bounded.

7. Statement and Prove Mean value theorem.

School of Science, Assignment Session 2021-22

Course Code: DCEMM-113	Course Title: Function of Complex	Maximum Marks : 30
	Variable	

(Section 'A')

(Long Answer Questions)

NOTE: Answer each question in 500 to 800 words. All carry equal marks.

Maximum Marks: 18

- 1. If $u = \frac{1}{2}\log(x^2 + y^2)$, find v such that f(z) = u + iv is analytic. Determine f(z) in terms of z.
- 2. Find the radius of convergence R of the following power series:

(i) $\sum_{n=0}^{\infty} z^n$ (ii) $\sum_{n=1}^{\infty} \frac{z^n}{n}$ (iii) $\sum_{n=1}^{\infty} \frac{z^n}{n^2}$

3. Using Cauchy integral formula, calculate the following integrals.

$$\int_{c} \frac{\cos(\pi z)}{z(z^{2}+1)} dz$$
, where *C* is the circle $|z| = 2$

4. Evaluate $\int_0^{3+i} z^2 dz$ along the line joining the points (0, 0) and (3, 1).

(Section – B)

(Short Answer Questions)

Maximum Marks: 12

Note: Answer each question in 200 to 300 Words. All carry equal marks.

5. Evaluate $\int_c \frac{dz}{z-2}$ for n = 2,3,4 ... where z = a is a point inside the simple closed curve c.

- 6. Find Taylor Series of $f(z) = \frac{1}{z}$ about z = -1, z = 1 and z = 2. Determine the circle of convergence in each case.
- 7. For the conformal transformation $w = z^2$. Show that the circle |z 1| = 1 transforms into the cardioid $R = 2(1 + \cos \emptyset)$ where $w = Re^{i\theta}$ in the *w*-plane.

School of Science, Assignment Session 2021-22

Course Code: SBSMM-03	Course Title: Elementary Analysis	Maximum Marks : 30

(Section 'A') (Long Answer Questions)

NOTE: Answer each question in 500 to 800 words. All carry equal marks.

Maximum Marks: 18

1. Write truth tables fo the sentence $P \Rightarrow P$ and

 $P \Rightarrow -P$. Is the First sentence a tautology.

2. The diagonal or the equality relation & *in a set S is an equivalence*

relation in S. For it $x, y \in S$ the x y iff x = y.

- **3**. Let x be a set. Consider the relation R in (e(x)), given by : for A, B $\in (e(n))$ ARB if A \subseteq B.
- **4**. Let $f: X \to Y$ be a map and let A and B subsets of X, then $A \subseteq B \Rightarrow f(A)$ $\subseteq f(B)$

(Section – B) (Short Answer Questions)

Maximum Marks: 12

Note: Answer each question in 200 to 300 Words. All carry equal marks.

5. Let
$$X = \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$$
, $y = [-1, 1]$

Let $f: X \to Y$ given by $f(x) = sinx, x \in X$.

6. Evaluate $\iint xy \, dx dy$ over the region in the positive quadrant for which $x + y \le 1$. 7. Find the volume inside the paraboloid $x^2 + 4z^2 + 8y = 16$ and on the positive side of xz -plane.